

lim [radice di n]! / $n^2 \ln(n)$
 $n \rightarrow \infty$

$$\lim_{n \rightarrow \infty} \frac{\lfloor \sqrt{n} \rfloor!}{n^2 \log n} = +\infty$$

$$n! \geq (n-5)^5 \leadsto \lfloor \sqrt{n} \rfloor! \geq (\lfloor \sqrt{n} \rfloor - 5)^5 \geq (\sqrt{n} - 6)^5$$

$$\frac{\lfloor \sqrt{n} \rfloor!}{n^2 \log n} \geq \frac{(\sqrt{n} - 6)^5}{n^2 \log n} \sim \frac{\sqrt{n}}{\log n} \rightarrow +\infty$$

lim [radice di $(n^2 + 1)$] - n
 $n \rightarrow \infty$

$$\lim_{n \rightarrow +\infty} \lfloor \sqrt{n^2 + 1} \rfloor - n = 0$$

$$n < \sqrt{n^2 + 1} < n + 1 \quad n^2 < (\sqrt{n^2 + 1})^2 < (n + 1)^2$$

$$\lfloor \sqrt{n^2 + 1} \rfloor = \lfloor n \rfloor = n$$

$$\lfloor \sqrt{n^2 + 1} \rfloor - n = 0$$